

# MATH 153

## Today

1. WeBWorK/Questions
2. 8.1 Sequences

### Goals:

1. 8.7 Taylor polynomials (Understand the extension of tangent line approximations to higher-order polynomial approximations)

## Where is today's material used?

1. Many physical phenomena modeled with complicated functions are approximated with polynomials.
2. Physics: period of a simple pendulum, electric dipoles.
3. Chemistry: Lennard-Jones potential.

## 8.7 Taylor Polynomials

1. In Calc I, we approximate functions with tangent lines. We will extend that idea to “tangent parabolas,” “tangent cubics,” etc.
2. **Definition:** Let  $f$  be a function with  $n$  continuous derivatives in an open interval containing  $a$ . The  **$n$ th-degree Taylor polynomial of  $f$  at  $a$**  is the polynomial

$$T_n(x) = f(a) + \frac{f'(a)}{1!}(x - a) + \frac{f''(a)}{2!}(x - a)^2 + \dots + \frac{f^{(n)}(a)}{n!}(x - a)^n.$$

3. Note that the linearization of  $f$  at  $a$  is  $T_1(x)$ . It's graph is the tangent line to  $f$  at  $x = a$ .

## Next Time

1. 8.1: Sequences.
2. **Turn in** 8.7 WeBWorK 01: 3, 5