

# MATH 253

## Today

1. Finish 5.3 Diagonalizability (Understand when a matrix is similar to a diagonal matrix and how to diagonalize it.)
2. Python 2
3. WeBWorK

### Where is today's material used?

1. Physics (quantum physics, principle axes, fluid dynamics, ...)
2. Economics
3. Math (differential equations, statistics, ...)

**Lemma 0.1.** *If  $A$  is similar to  $B$ , say  $B = S^{-1}AS$ , and  $X$  is an eigenvector of  $B$  corresponding to  $\lambda$ , then  $SX$  is an eigenvector of  $A$  corresponding to  $\lambda$ .*

**Theorem 1.** *Let  $A$  be an  $n \times n$  matrix. Then  $A$  is similar to a diagonal matrix  $D$  if and only if  $A$  has  $n$  linearly independent eigenvectors. In this case, if the eigenvectors are  $v_1, \dots, v_n$  corresponding to  $\lambda_1, \dots, \lambda_n$ , then with  $S = [v_1 \dots v_n]$ ,  $S^{-1}AS = D = \text{diag}(\lambda_1, \dots, \lambda_n)$ .*

## Next Time

1. 5.4 Page Rank
2. 1 proof due today (5.2: 10)
3. 3 proofs due Wednesday (5.3: 17, 18, 19)