

Solutions to Homework Assignment 33

MATH 345

Section 73, Page 224

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1. For $\frac{e^z}{z(z^2 + 1)}$, we have

$$\begin{aligned}\frac{1}{z} \left(\sum_{n=0}^{\infty} \frac{z^n}{n!} \right) \left(\sum_{m=0}^{\infty} (-z^2)^m \right) &= \frac{1}{z} \left(\sum_{n=0}^{\infty} \frac{z^n}{n!} \right) \left(\sum_{m=0}^{\infty} (-1)^m z^{2m} \right) \\ &= \frac{1}{z} \left(1 + z + \frac{z^2}{2} + \frac{z^3}{6} + \dots \right) (1 - z^2 + z^4 - \dots) \\ &= \frac{1}{z} \left(1 + z + \left(\frac{z^2}{2} - z^2 \right) + \left(\frac{z^3}{6} - z^3 \right) + \dots \right) \\ &= \frac{1}{z} + 1 - \frac{z}{2} - \frac{5z^2}{6} + \dots\end{aligned}$$

3. Ugh. Not gonna try to \LaTeX this one...