

CS 145 Images and Imagination

Practice Problems for Exam 2

1. String concatenation: Complete the `println` instruction so that the output of

```
for (int i =0; i < 10; i++) {
    int num = (int) random(100);
    println("i = " + i + ": The random number is " + num); //finish
}
```

2. For the function below:

- a. What is the return type? float
- b. What is the *name* of the parameter? red
- c. What is the *type* of the parameter? int
- d. Which of the following are legal ways (or reasonable) *to call* the function?

- i. `float r = convertRed();` // bad - no parameter
- ii. `int r = convertRed(2.5);` // bad - wrong type for return
// and parameter
- iii. `float r = convertRed(155);` // ok
- iv. `convertRed(100);` // syntax ok but nothing done
// with return value
- v. `stroke(convertRed(100), 1.0, 1.0);` // ok

3. To set a color in Processing, you use the command `stroke(r,g,b)`. To set a grayscale value, you just use a single number `stroke(g)` where `g` can be computed from the RGB value by adding together 30% of the red value, 59% of the green value, and 11% of the blue value. For example, if `r=10` (out of 255), `g=100`, and `b = 255`, then the grayscale value will be $g = (0.3*10)+(0.59*100)+((0.11*255) = 90.2$. Write a function that takes the three `rgb` integer values as parameters, and returns the grayscale value as a float.

```
float calcGray(int r, int g, int b) {
    float gray = 0.3*r + 0.59*g + 0.11*b;
    return gray;
}
```

4. Complex numbers: Place the following in standard form $a + b i$.
- i^3 $\underline{\hspace{2cm}} - i \underline{\hspace{2cm}}$
 - $\sqrt{-36} + 3 i^2$ $\underline{\hspace{2cm}} - 3 + 6 i \underline{\hspace{2cm}}$
5. Complex numbers: Given $z_1 = -1 + 7 i$ and $z_2 = (2 + i)$. Calculate the following, placing the result in standard form
- $z_1 + z_2 = \underline{\hspace{1cm}} 1 + 8 i \underline{\hspace{1cm}}$
 - $z_1 - z_2 = \underline{\hspace{1cm}} -3 + 6 i \underline{\hspace{1cm}}$
 - $2 z_1 = \underline{\hspace{1cm}} -2 + 14 i \underline{\hspace{1cm}}$
 - $z_1 z_1 = z_1^2 = \underline{\hspace{1cm}} -48 - 14 i \underline{\hspace{1cm}}$
 - $z_1 z_2 = \underline{\hspace{1cm}} -9 + 13 i \underline{\hspace{1cm}}$
 - $\bar{z}_1 + z_1 = \underline{\hspace{1cm}} -2 \underline{\hspace{1cm}}$
 - $\bar{z}_1 z_1 = \underline{\hspace{1cm}} 50 \underline{\hspace{1cm}}$
 - Length of $z_1 = |z_1| = \underline{\hspace{1cm}} \sqrt{50} \underline{\hspace{1cm}}$
6. Class syntax: In class, we made use of a Complex class in Processing to compute the Mandelbrot set.
- How would you create a new Complex object with real component equal to 1.5 and imaginary component equal to -6 ?

Complex c = new Complex(1.5, -6);
 - In Processing, suppose you have created complex numbers c1, c2, and c3. How do you multiply c1 and c2 together, placing the result in c3?

c3 = Complex.cMult(c1, c2);
 - In Processing, suppose you have created complex numbers c1, c2, and c3. How do you compute (i.e. what is the syntax of) for computing
 $c3 = c1 * c2 + c1$

c3 = Complex.cAdd(Complex.cMult(c1, c2) , c1);

What is the standard form for the complex numbers whose values in polar coordinates are

d. $r = 2, \theta = 90^\circ$ 2 i

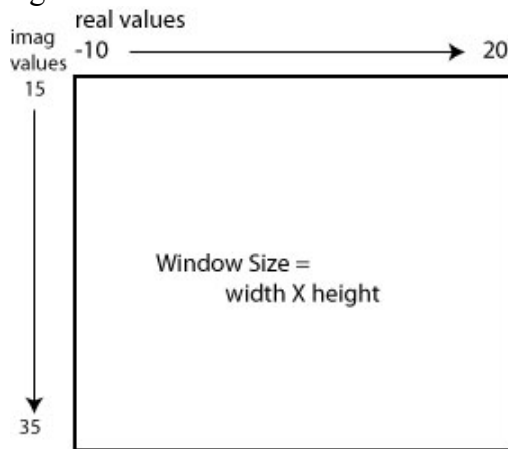
e. $r = 1, \theta = 180^\circ$ - 1

7. What is the polar coordinate representation (r, θ) for the following complex numbers

a. $-3 i$ (r, \theta) = (3, 270)

b. $1 + i$ (r, \theta) = (\sqrt{2}, 45)

8. Rescaling: Given a region of the complex plane where the real component ranges between -10 and 20, and the imaginary part ranges between 15 and 35 as shown in the figure:



a. How does one use the map function to determine the pixel location of the complex number
 $z = 5 + 21 i$.

```
int pixeli = map(5, -10, 20, 0, width );
int pixelj = map(21, 15, 35, 0, height );
```

b. How does one use the map function to determine the complex number corresponding to the pixel (i,j)

```
int real = map(i, 0, width, -10, 20);
int imag = map(j, 0, height, 15, 35);
```

9. Convert the following for-loop to a while loop:

```
for (int i =0; i < 100; i++) {
    println(i);
}
```

```
int i = 0;
while (i < 100) {
    println(i);
    i++;
}
```

10. Mandelbrot Set: Write a do-while loop that iterates on the complex function $z = z^2 + c$. It stops when either the loop has iterated 100 times or the length of z exceeds 2. Initialize z and c to be $z=0$ and $c = 0.5 + i$.

```
int k = 0;
do {
    z = Complex.cAdd( Complex.cMult(z, z) , c );
    k++;
} while ( k < 100 && Complex.len(z) < 2);
```

11. Recursion: Write a recursive function to output the numbers from 0 to 100 *in reverse order*.

```
void setup() {
    printNums(100);
}

void printNums(int n) {
    if (n < 0) {
        return;
    }
    else {
        println(n);
        printNums(n-1);
    }
}
```

12. Recursion: Write a recursive function to add the numbers from 1 to n , for some value of n .

```
void setup() {
    int n = 100;
    println ("The sum from 1 to "+ n + " is " + addNums(n));
}

int addNums(int n) {
    if (n <= 0) {
        return 0;
    }
    else {
        return n + addNums(n-1);
    }
}
```