

**Complex Number Exercises**  
*CS 145 Images and Imagination*  
*Spring 2010*

1. Put in  $z$  standard form ( $a + b i$ ):
  - a.  $z = 4 + \sqrt{9} =$  \_\_\_\_\_
  - b.  $z = i^2 + i\sqrt{25} =$  \_\_\_\_\_
  - c.  $z = 254 i^2 =$  \_\_\_\_\_
  - d.  $z = i^7 =$  \_\_\_\_\_
2. Convert from polar to standard form (Cartesian coordinates) in standard form
  - a.  $r = 4, \theta = 25, z =$  \_\_\_\_\_
  - b.  $r = 5, \theta = 165, z =$  \_\_\_\_\_
3. Compute the modulus (length) of
  - a.  $z = 3 + 4i, r =$  \_\_\_\_\_
  - b.  $z = -2 + 1.6i, r =$  \_\_\_\_\_
4. What is the  $\bar{z} =$  complex conjugate of each of the  $z$  values in problem 1
  - a.  $\bar{z} =$  \_\_\_\_\_
  - b.  $\bar{z} =$  \_\_\_\_\_
  - c.  $\bar{z} =$  \_\_\_\_\_
  - d.  $\bar{z} =$  \_\_\_\_\_
5. Suppose  $z_1 = (4 + 3 i)$  and  $z_2 = (-2 + 4 i)$ . Calculate the following, placing the result in standard form
  - a.  $z_1 + z_2 =$  \_\_\_\_\_
  - b.  $z_1 - z_2 =$  \_\_\_\_\_
  - c.  $2 z_1 =$  \_\_\_\_\_
  - d.  $z_1 z_1 = z_1^2 =$  \_\_\_\_\_
  - e.  $z_1 z_2 =$  \_\_\_\_\_
  - f.  $\bar{z}_1 + z_1 =$  \_\_\_\_\_
  - g.  $\bar{z}_1 z_1 =$  \_\_\_\_\_
  - h.  $z_1 / z_2 =$  \_\_\_\_\_