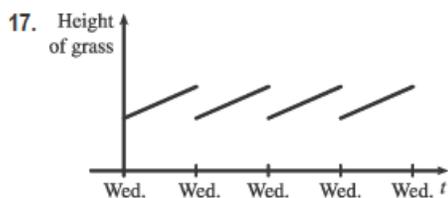
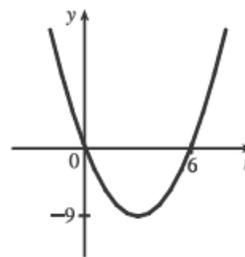

Homework1 Solutions

1. (a) The point $(-1, -2)$ is on the graph of f , so $f(-1) = -2$.
- (b) When $x = 2$, y is about 2.8, so $f(2) \approx 2.8$.
- (c) $f(x) = 2$ is equivalent to $y = 2$. When $y = 2$, we have $x = -3$ and $x = 1$.
- (d) Reasonable estimates for x when $y = 0$ are $x = -2.5$ and $x = 0.3$.
- (e) The domain of f consists of all x -values on the graph of f . For this function, the domain is $-3 \leq x \leq 3$, or $[-3, 3]$.
The range of f consists of all y -values on the graph of f . For this function, the range is $-2 \leq y \leq 3$, or $[-2, 3]$.
- (f) As x increases from -1 to 3 , y increases from -2 to 3 . Thus, f is increasing on the interval $[-1, 3]$.
5. No, the curve is not the graph of a function because a vertical line intersects the curve more than once. Hence, the curve fails the Vertical Line Test.
6. Yes, the curve is the graph of a function because it passes the Vertical Line Test. The domain is $[-2, 2]$ and the range is $[-1, 2]$.
7. Yes, the curve is the graph of a function because it passes the Vertical Line Test. The domain is $[-3, 2]$ and the range is $[-3, -2) \cup [-1, 3]$.
8. No, the curve is not the graph of a function since for $x = 0, \pm 1$, and ± 2 , there are infinitely many points on the curve.



28. $f(x) = (5x + 4)/(x^2 + 3x + 2)$ is defined for all x except when $0 = x^2 + 3x + 2 \Leftrightarrow 0 = (x + 2)(x + 1) \Leftrightarrow x = -2$ or -1 , so the domain is $\{x \in \mathbb{R} \mid x \neq -2, -1\} = (-\infty, -2) \cup (-2, -1) \cup (-1, \infty)$.

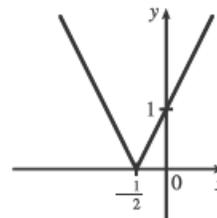
35. $f(t) = t^2 - 6t$ is defined for all real numbers, so the domain is \mathbb{R} , or $(-\infty, \infty)$. The graph of f is a parabola opening upward since the coefficient of t^2 is positive. To find the t -intercepts, let $y = 0$ and solve for t .
 $0 = t^2 - 6t = t(t - 6) \Rightarrow t = 0$ and $t = 6$. The t -coordinate of the vertex is halfway between the t -intercepts, that is, at $t = 3$. Since $f(3) = 3^2 - 6 \cdot 3 = -9$, the vertex is $(3, -9)$.



$$38. F(x) = |2x + 1| = \begin{cases} 2x + 1 & \text{if } 2x + 1 \geq 0 \\ -(2x + 1) & \text{if } 2x + 1 < 0 \end{cases}$$

$$= \begin{cases} 2x + 1 & \text{if } x \geq -\frac{1}{2} \\ -2x - 1 & \text{if } x < -\frac{1}{2} \end{cases}$$

The domain is \mathbb{R} , or $(-\infty, \infty)$.



48. $x^2 + (y - 2)^2 = 4 \Leftrightarrow (y - 2)^2 = 4 - x^2 \Leftrightarrow y - 2 = \pm\sqrt{4 - x^2} \Leftrightarrow y = 2 \pm \sqrt{4 - x^2}$. The top half is given by the function $f(x) = 2 + \sqrt{4 - x^2}$, $-2 \leq x \leq 2$.

3. (a) (graph 3) The graph of f is shifted 4 units to the right and has equation $y = f(x - 4)$.

(b) (graph 1) The graph of f is shifted 3 units upward and has equation $y = f(x) + 3$.

(c) (graph 4) The graph of f is shrunk vertically by a factor of 3 and has equation $y = \frac{1}{3}f(x)$.

(d) (graph 5) The graph of f is shifted 4 units to the left and reflected about the x -axis. Its equation is $y = -f(x + 4)$.

(e) (graph 2) The graph of f is shifted 6 units to the left and stretched vertically by a factor of 2. Its equation is $y = 2f(x + 6)$.

10. $y = 1 - x^2 = -x^2 + 1$: Start with the graph of $y = x^2$, reflect about the x -axis, and then shift 1 unit upward.

