## Correlation

The **correlation** between two quantitative variables measures the strength and direction of their linear relationship, expressed by the **correlation coefficient** *r*.

$$r = \frac{\Sigma(z_x z_y)}{n-1}$$



## Facts about the correlation coefficient r

- 1. If *r* is positive, the scatterplot goes up from left to right. If *r* is negative, the scatterplot goes down from left to right.
- 2. *r* is always between -1 (perfect negative correlation) and 1 (perfect positive correlation). *r*=0 means no correlation.







- 3. Switching the variables has no effect on *r*.
- 4. Shifting or stretching the data has no effect on r.
- 5. Correlation has no units.
- 6. Correlation is sensitive to outliers.

- 7. Correlation does not imply causation!
- 8. Non-linear relationships can have strange correlations. Four possibilities:
  - a) Scatterplot is linear and tightly packed: high correlation
  - b) Scatterplot is linear and cloud-shaped: low correlation
  - c) Scatterplot is curved and tightly packed: high association, but we need to calculate *r* differently.
  - d) Scatterplot is curved and cloud-shaped: low association, but we need to calculate *r* differently.

