

# Josh Laison

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he/him

## Research interests

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Graph theory and discrete geometry, focusing on geometric representations of graphs.

## Education

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Ph.D. Mathematics, 2001, Dartmouth College

A.M. Mathematics, 1999, Dartmouth College

B.A. Mathematics, 1996, Oberlin College

## Teaching experience

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Professor, Willamette University, 2018-present

Associate Professor, Willamette University, 2011-2018

Assistant Professor, Willamette University, 2007-2011

Visiting Assistant Professor, St. Olaf College, 2006-2007

Visiting Assistant Professor, Colorado College, 2002-2006

Visiting Assistant Professor, Kenyon College, 2001-2002

## Courses taught (2011-present)

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College Colloquium Tabletop Game Design; College Colloquium Technically Speaking; Math 130 Contemporary Mathematics; Math 138 Statistics; Math 142 Calculus 2; Math 163 Discrete Mathematics; Math 249 Multivariable Calculus; Math 251W Foundations of Advanced Mathematics; Math 253 Linear Algebra; Math 376 Graph Theory; Math 399 Junior Seminar in Mathematics; Math 456 Abstract Algebra I; Math 470 Topology; Math 476 Modern Geometry; MATH 498 Senior Research Seminar I; Math 499W Senior Research Seminar II

## Undergraduate research collaborations (2017-present)

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Prior to 2017 I mentored 17 additional undergraduate research projects with 26 students. My undergraduate collaborators are indicated with a \*.

- **Visibility Fractions of Polyomino Visibility Graphs** with Taden Bowden\*, and Brooks Danielson\*, Willamette Mathematics Senior Thesis

- **Variations of Polyomino Visibility Graphs** with Ezekiel Druker\* and Chris Olivia\*, Willamette Mathematics Senior Thesis
- **3D Polyomino Visibility Graphs** with Dayton Roberts\*, and Benjamin Weber\*, Willamette Mathematics Senior Thesis
- **Polyomino Visibility Graphs** with Ezekiel Druker\*, Clemency Little\*, Chris Olivia\*, Dayton Roberts\*, and Benjamin Weber\*, Willamette Mathematics Junior Thesis
- **Corner Rectangle Visibility Graphs** with August Bergquist\*, Juni DeYoung\*, Ezekiel Jakob Druker\*, Jayden Li\*, and Lani Southern\*, Willamette Mathematics Junior and Senior Thesis
- **Chromatic Peg Solitaire on Graphs** with Ren Daubert\*, Gigi Hewitt\*, and Corinne Pierson\*, Willamette Mathematics Senior Thesis
- **Optimal  $k$ -solvable Peg Solitaire** with Taylor Gruber\* and Adaela Shearer\*, Willamette Mathematics Senior Thesis
- **Isometric Fixing Numbers of Graphs** with Nathan I. Howard\* and Alexandra N. Walker\*, Willamette Mathematics Senior Thesis
- **Polynomial Difference Graphs** with Steven Howley\* and Paige Murray\*, Willamette Mathematics Senior Thesis
- **A Variation of Peg Solitaire on Graphs** with Connor Crowley\* and Justin Scanlon\*, Willamette Mathematics Senior Thesis
- **Graphs Represented by Edge Intersections of Paths on Grids and Uniform Tilings** with Johannes Griesser\* and Lucas Perryman-Deskins\*, Willamette Mathematics Senior Thesis
- **Super Tuple Edge-Magic Total Graphs** with Gus Mayeno\*, Gillian Pringle\*, and Lydia Savelli\*, Willamette Mathematics Senior Thesis
- **Intersection Graphs of Maximal Convex Sub-Polygons** with Caroline Daugherty\*, Rebecca Robinson\*, and Kyle Salois\*, funded through the Willamette Valley Consortium REU grant
- **Creating Problems** with Zechariah Hazel\*, Peri Hildum\*, Allison Kerkhoff\*, Cayla Skillin-Brauchle, and Arthur Stamey-Mills\*, funded through a Willamette University Liberal Arts Research Collective (LARC) Summer Research Collaboration Grant
- **Playtesting, Illustration, and Game Publishing** with Dana Kehrley\*, funded through a Willamette University College Colloquium Research Grant
- **Weighted  $k$ -Majority Tournaments** with Jeremy Coste\* and Dane Miyata\*, Willamette Mathematics Senior Thesis
- **Transport Pebbling** with Megan Duff\*, Ivy MacDuff\*, Kees McGahan\*, and Colin Starr, Willamette Mathematics Senior Thesis

- **The Accountable Art Gallery Problem** with Samuel Coste\* and Boyuan Lyu\*, Willamette Mathematics Senior Thesis
- **Efficient Pentamino Folding** with Taylor Matsumura\*, Rufei Men\*, and Mattie Wiltbank\*, Willamette Mathematics Senior Thesis
- **Mountain Graphs in Origami Crease Patterns** with Katy Ohsiek\* and Ana Wright\*, Willamette Mathematics Senior Thesis

## Publications

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My undergraduate co-authors are indicated with a \*.

1. **Approval Gap of Weighted  $k$ -Majority Tournaments**  
with Jeremy Coste\*, Breeann Flesch, Erin McNicholas, and Dane Miyata\*, *Theory and Applications of Graphs* **11**, no. 1 (May 2024).
2. **Area, Perimeter, Height, and Width of Rectangle Visibility Graphs**  
with John S. Caughman, Charles Dunn, Nancy Ann Neudauer, and Colin L. Starr, *Journal of Combinatorial Optimization* **46**, no. 18 (October 2023).
3. **Intersection Graphs of Maximal Sub-polygons of  $k$ -Lizards**  
with Caroline Daugherty\*, Rebecca Robinson\*, and Kyle Salois\*, *Graphs and Combinatorics* **39**, no. 75 (June 2023).
4. **Graph Stamping: Art-Inspired Mathematics**  
with Zechariah Hazel\* and Allison Kerkhoff\*, *Math Horizons* **28**, no. 4 (April 2021), 24–27.
5. **Base Size Sets and Determining Sets**  
with Erin McNicholas and Nicole Seaders, *Discrete Mathematics* **342**, no. 11 (November 2019), 2994–2999.
6. **Prime Power and Prime Product Distance Graphs**  
with Yumi Kaneda\*, Jeffrey Schreiner-McGraw\*, and Colin Starr, *Discrete Applied Mathematics* **255** (February 2019), 334–338.
7. **Weighted Pebbling Numbers of Graphs**  
with Stephanie Partlow\*, Cameron McLeman, and Kathryn Nyman, *Journal of Combinatorial Mathematics and Combinatorial Computing* **100** (February 2017), 223–244.
8. **Critical Pebbling Numbers of Graphs**  
with Courtney R. Gibbons\* and Erick J. Paul\*, *Journal of Combinatorial Mathematics and Combinatorial Computing* **99** (November 2016), 199–224.
9. **Finite Prime Distance Graphs and 2-Odd Graphs**  
with Colin Starr and Andrea Walker\*, *Discrete Mathematics* **313** (October 2013), no. 20, 2281–2291.

10. **More Directions in Visibility Graphs**  
with Ellen Gethner, *Australasian Journal of Combinatorics* **50** (2011), 55–65.
11. **Subspace Intersection Graphs**  
with Yulan Qing\*, *Discrete Mathematics* **310** (2010), no. 23, 3413-3416.
12. **Triangle, Parallelogram, and Trapezoid Orders**  
with Kenneth P. Bogart and Stephen P. Ryan, *Order* **27** (2010), no. 2, 163-175.
13. **Obstacle Numbers of Graphs**  
with Hannah Alpert\* and Christina Koch\*, *Discrete and Computational Geometry* **44** (2010), no. 1, 223-244.
14. **Fixing Numbers of Graphs and Groups**  
with Courtney R. Gibbons\*, *Electronic Journal of Combinatorics* **16** (2009), no. 1 (electronic).
15. **Dual Unfoldings of Polyhedra**  
with John J. Watkins and Lucian Wilson\*, *Congressus Numerantium* **191** (2008), 161-172.
16. **Unit and Proper Tube Orders**  
*Order* **25** (2008), no. 3, 237-242.
17. **Seeing Dots: Visibility of Lattice Points**  
with Michelle Schick\*, *Mathematics Magazine* **80** (2007), no. 4, 274–282.
18. **Bar  $k$ -Visibility Graphs**  
with Alice Dean, William Evans, Ellen Gethner, Mohammad A. Safari, and William T. Trotter, *Journal of Graph Algorithms and Applications* **11** (2007) no. 1, 45-59.
19. **Tube Representations of Ordered Sets**  
*Order* **21** (2004), no. 3, 209-232.
20. **Free Triangle Orders**  
*Order* **20** (2003), no. 2, 99-108.
21. **Comparability Invariance Results for Tolerance Orders**  
with Kenneth P. Bogart, Garth Isaak, and Ann N. Trenk, *Order* **18** (2001), no. 3, 281-294.

## Conference proceedings.....

22. **Minimum Representations of Rectangle Visibility Graphs (Extended Abstract)**  
with John S. Caughman, Charles Dunn, Nancy Ann Neudauer, and Colin L. Starr, in Patrick Healy and Nikola S. Nikolov, editors, *Graph Drawing*, volume 8871 of *Lecture Notes in Computer Science*, Springer-Verlag, Berlin, 2014. Revised papers from the 22nd International Symposium on Graph Drawing (GD2014), Würzburg, Germany, September 2014, 527–528.
23. **Bar  $k$ -Visibility Graphs: Bounds on the Number of Edges, Chromatic Number, and Thickness (Extended Abstract)**  
with Alice Dean, William Evans, Ellen Gethner, Mohammad A. Safari, and William T. Trotter,

in Patrick Healy and Nikola S. Nikolov, editors, *Graph Drawing*, volume 3843 of *Lecture Notes in Computer Science*, Springer-Verlag, Berlin, 2006. Revised papers from the 13th International Symposium on Graph Drawing (GD2005), Limerick, Ireland, September 2005, 73–82.

## Expository articles.....

24. **My Experiences Researching With Undergraduate Mathematicians: The Collaboration Model**  
in Joseph A. Gallian, editor, *Proceedings of the Conference on Promoting Undergraduate Research in Mathematics*, American Mathematical Society, 2007.

## Submitted.....

25. **Veto Interval Graphs**  
with Breeann Flesch, Jessica Kawana\*, Dana Lapidés\*, and Stephanie Partlow, submitted in August 2022 to *Graphs and Combinatorics*

## In progress.....

26. **Triangle Visibility Graphs** with John S. Caughman, Charles Dunn, Nancy Ann Neudauer, and Colin L. Starr
27. **Corner Rectangle Visibility Graphs** with Juni DeYoung\*, Jayden Li\*, and Lani Southern\*
28. **Mountain Graphs in Origami Crease Patterns**  
with Breeann Flesch, Erin McNicholas, Katy Ohsiek\* and Ana Wright\*

## Professional activities

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### Grants and Awards.....

- Willamette University Liberal Arts Research Collective (LARC) Summer Research Collaboration Grant with Cayla Skillin-Brauchle, summer 2017
- Principal Investigator, NSF Willamette Mathematics Consortium REU Grant, funding 27 students and 9 faculty in summer research 2015–2017
- Faculty mentor, NSF Willamette Mathematics Consortium REU Grant, summers 2008, 2012, 2014, 2017
- Project NExT (New Experiences in Teaching) Fellow, 2002-2003, Mentor, 2021-2022
- Faculty Merit Award for Teaching, Willamette University College of Liberal Arts, Academic year 2009–2010
- 12 additional internal Willamette University grants awarded for research and course development (Atkinson Research Grant, Hewlett Curriculum Development Grant, College Colloquium Research Grant, Research Travel Grant, Course Development Grant).

## Conferences Organized.....

- MOVES (Mathematics of Various Entertaining Subjects), National Museum of Mathematics, New York, NY, August 2015, August 2017, August 2019, August 2022, August 2023
- Mini-MOVES Gathering, New York, NY and remote, February 2022
- MOVES Meet-up, August 2021, remote
- SSRD (Student Scholarship Recognition Day), Willamette University, April 2018, April 2019, and April 2020
- NUMS (Northwest Undergraduate Mathematics Symposium), Willamette University, November 2018
- Pacific Northwest Section Meeting of the Mathematical Association of America, Willamette University, April 2013
- Pikes Peak Regional Undergraduate Mathematics Conference, Colorado College, February 2005
- Rocky Mountain Discrete Math Days, Colorado College, August 2004
- Rocky Mountain Section Meeting of the Mathematical Association of America, Colorado College, April 2004

## Art Exhibitions.....

- *Point of View*, Hallie Ford Museum of Art, September 2018–September 2019
- *Creating Problems: A Liberal Arts Research Community*, Willamette University, September 2017

## Equity, Diversity, and Inclusion.....

- Funded participant, Quantitative Reasoning Summer Learning Circle: Data Deep Dive into BIPOC Representation in Computing and Data Science, Summer 2023
- Participant, Math Leaders 4 Racial Justice Workshop, University of Texas at Austin (remote), Summer 2022
- Participant, Northwest Five Consortium (NW5C) Historical Representations of Racism and Exclusionism Summer Learning Community, June-August 2021
- Attendee, ParaDIGMS (Diversity in Graduate Mathematical Sciences) Conference, April 2021 and April 2022 (remote)
- Organizer, Willamette Mathematics Department discussion group on advocating for students of color in mathematics, 2021-2023
- Member, Willamette University President's Task Force on Equity and Inclusion, 2016–2017

## Other.....

- Mathematical Association of America Beckenbach Book Prize Committee (awarding a prize for a book published by the MAA each year), 2022-present
- Reviewer for the *Journal of Graph Algorithms and Applications*, *Discrete Mathematics*, *PRIMUS: Problems, Resources, and Issues in Mathematics Undergraduate Studies*, and *Order*
- Board member, MathILy Advisory Amalgam (summer program for mathematically excellent secondary students)
- Local organizer, MegaMenger community art installation project, October 2014
- Attended 18 teaching workshops
- Organized 13 conference sessions, panels, workshops, and seminars
- Organized and wrote six mathematical problem solving competitions
- Wrote 14 reviews for the Mathematical Reviews database (online as mathscinet)

## Service to Willamette University

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- Willamette University Accreditation Committee, 2022-present
- Learning Assessment Committee, Chair 2022-present, Member 2021-2022
- Chair, Student Scholarship Recognition Day Committee, 2017-2020
- Mathematics Department Chair, 2012-2015 and Fall 2019
- Big Questions General Education Working Group, 2018
- Organizer, Mathematics Department External Review, March 2018
- Teacher, Willamette Academy Summer Camp, July 2018, July 2019, July 2021, July 2023
- Committee for Faculty Development, 2015-2017
- Writing Program Advisory Committee, 2011-2012
- College of Liberal Arts Faculty Secretary, 2009-2010
- Faculty Colloquium Committee, 2008-2010
- Twelve Hiring Committees
- Advisor for student groups: Pi Mu Epsilon National Honorary Society 2008-present, Math Club 2015-present, Board Game Club 2023-present, Esports Club 2018-2022, Millstream Board

Games Collective 2021–2022, Board and Card Game Coalition, 2011–2014, Games Unplugged, 2016–2017.

- Organizer, Annual Pacific Northwest Intercollegiate Ginormous Blokus Tournament, 2011-2019, 2024

## Presentations (2017-present)

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Prior to 2017 I gave 89 additional conference presentations and colloquium talks.

### Conference presentations

1. Gathering for Gardner, *Graphs of Rectangles Looking Diagonally*, Atlanta, GA, [February 2024]
2. Invited speaker, Pacific Northwest Section Meeting of the Mathematical Association of America, Special Session on Undergraduate Research, *Finding a Student Research Topic in Graph Theory: The Lightning Round*, Newberg, OR, April 2023
3. Invited speaker, Joint Mathematics Meetings, Special Session on Presenting Research Mathematics through Visual Storytelling: Slides without Words and Equations, *Intersection graphs of convex sub-polygons of a polygon, a story in pictures*, April 2022
4. Joint Mathematics Meetings, *Stamping Numbers of Graphs*, Denver, CO, January 2020
5. SIAM Discrete Mathematics Conference, *Variations on the Graph Pebbling Game*, June 2018
6. Joint Mathematics Meetings, *Veto Interval Graphs and Variations*, San Diego, CA, January 2018
7. Coast Combinatorics Conference, *Determining Sets and Base Size Sets of Groups*, Kona-Kailua, HI, February 2017
8. Joint Mathematics Meetings, *Base Size Sets and Determining Sets*, Atlanta, GA, January 2017

### Public communication and outreach

9. Skype a Scientist, *Graph Theory*, Venice High School, May 2024 (12th grade class)
10. Bay Area Mathematics Adventures, *Puzzles in Geometric Graph Theory*, May 2023 (General audience)
11. Skype a Scientist, *Graph Theory*, Snoqualmie Elementary School, April 2022 (3rd grade class)
12. Willamette University Faculty Colloquium, *Scaling Lizards and Seeing Rectangles: Two Problems in Geometric Graph Theory*, February 2022 (Non-STEM faculty)
13. Hua Summer Math Workshop, *Circuit Crossing Puzzles*, July 2021 (K-12 math teachers)
14. Skype a Scientist, *Graph Theory*, Murtaugh Elementary School, April 2021 (4th grade class)



15. Skype a Scientist, *Graph Theory*, Leighton Elementary School, December 2020 (4th grade class)
16. Willamette University Faculty Summer Workshop, *Encouraging Students to Think Outside the Box Using Lessons from Music and Math*, July 2020, co-presented with James Miley (Non-STEM faculty)
17. Hua Summer Math Workshop, *Pebbling Problems and Puzzles*, June 2020 (K-12 math teachers)
18. Hua Summer Math Workshop, *The Chaos Game*, June 2020 (K-12 math teachers)
19. Skype a Scientist, *Graph Theory Problems and Applications*, Silver Creek Central School, June 2020 (two presentations, 9th and 10th grade math classes)
20. Family Weekend Mini-University Session, Willamette University, *Exploring Graph Pebbling Puzzles and Problems*, October 2019 (Parents of Willamette students)
21. Family Weekend Mini-University Session, Willamette University, *Exploring Graph Pebbling Puzzles and Problems*, October 2017 (Parents of Willamette students)

## Colleges and universities

22. Lewis and Clark Mathematical Sciences Colloquium, *Scaling Lizards and Seeing Rectangles: Two Problems in Geometric Graph Theory*, October 2021
23. Mathematics Department Colloquium, Willamette University, *Distinguishing, Determining, Fixing, Stamping, and Otherwise Breaking Graph Symmetries*, March 2019
24. Mathematics Department Colloquium, Pacific University, *Prime Distance Graphs*, November 2018
25. Mathematics Department Colloquium, Willamette University, *Prime Distance Graphs*, October 2018
26. Featured speaker, Pi Mu Epsilon Induction Ceremony, Western Oregon University, *Variations of Graph Pebbling*, May 2017
27. Northwest Undergraduate Mathematics Symposium (NUMS), *Puzzling Showdown*, McMinnville, OR, April 2017
28. Math Club Seminar, Carnegie Mellon University, *Star Numbers of Geometric Shapes*, March 2017